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| I. | Factoring |
| II. | Completing the Square |
| III. | Quadratic Formula |
| IV. | Square Roots |

Solve using any method. List what methods you can use to solve each one.

4 1. $x^2 - 2x - 15 = 0$ ^{Not 3x}

I, II, III

$x = 5, -3$

2. $3x^2 - 4x - 2 = 0$

III

$\frac{4 \pm 2\sqrt{10}}{6}$

$\frac{2 \pm \sqrt{10}}{3}$

3. $4x^2 - 121 = 0$

I, III, IV

$\sqrt{x^2} = \pm \sqrt{\frac{121}{4}}$

$x = \pm \frac{11}{2}$

4. $(x-5)^2 = -4$ **IV**

$= \pm 2i$

$5 \pm 2i$

Factor:

5. $3x^2 - 10x - 8$

$(3x+2)(x-4)$

6. $25x^2 + 30x + 9$

$(5x+3)(5x+3)$

7. $36x^2 - 81$

$9(4x^2 - 9)$

$9(2x+3)(2x-3)$

Find the discriminant and describe the number and type of solutions to the quadratic equation.

8. $3x^2 - 25x + 13 = 0$

$(-25)^2 - 4(3)(13)$

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9. $5x^2 - 7x + 9 = 0$

$(-7)^2 - 4(5)(9)$

-131 **2 IMAGINARY**

Simplify:

10. $\sqrt{-98}$

$7i\sqrt{2}$

11. $\sqrt{-529}$

$23i$

12. $\sqrt{-63}$

$3i\sqrt{7}$

Simplify, then write answer in standard form.

13. $3i - (5 + 2i) - 12i + 15$

$3i - 5 - 2i - 12i + 15$

$10 - 11i$

14. $(4 - 5i) - (12 + 9i)$

$4 - 5i - 12 - 9i$

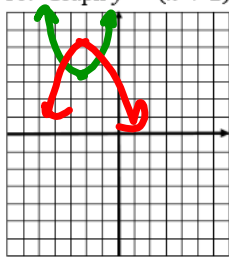
$-8 - 14i$

15. $(5 - 2i)(6 + 12i)$ $*i^2 = -1$

$30 + 60i - 12i - 24i^2$

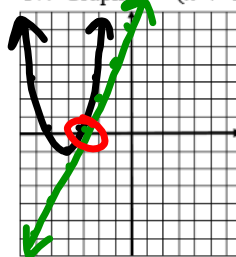
$54 + 48i$

16. Graph $y = (x + 2)^2 + 3$ and $y = -(x + 2)^2 + 5$. Solve the system of equations.



$(-3, 4)$ $(-1, 4)$

17. Graph $y = (x + 4)^2 - 1$ and $y = 2x + 6$. Solve the system of equations.



$(-3, 0)$

18. A tall tower is located in New Jersey City. The equation $f(t) = -16t^2 + 1296$ models the height $f(t)$ (in feet) of an object t seconds after it is dropped from the top of the tower.

a. What is the value of the height $f(t)$ when the object hits the ground? 0 ft

b. After how many seconds will the object hit the ground? 9 sec

$$0 = -16t^2 + 1296$$

c. What is the maximum height of the object? 1296 ft

d. What is the height of the object after 5 seconds? 896

$$f(5) = -16(5)^2 + 1296$$

Solve the system of equations.

19. $y = (x - 2)^2$ & $y = -x^2 + 4x - 2$

$$\begin{aligned} (x-2)^2 &= -x^2 + 4x - 2 \\ x^2 - 4x + 4 &= -x^2 + 4x - 2 \\ 2x^2 - 8x + 6 &= 0 \\ 2(x^2 - 4x + 3) &= 0 \\ 2(x-3)(x-1) &= 0 \\ x=3 & \quad x=1 \\ y=(3-2)^2=1 & \quad y=(1-2)^2=1 \\ \boxed{(3,1)} & \quad \boxed{(1,1)} \end{aligned}$$

20. $x^2 - 6x + y = -10$
 $3x^2 + 18x - y = +2$

$$\begin{aligned} + & \quad \quad \quad + \\ \hline 4x^2 + 12x &= -8 \\ 4x^2 + 12x + 8 &= 0 \\ 4(x^2 + 3x + 2) &= 0 \\ 4(x+2)(x+1) &= 0 \\ x=-2 & \quad x=-1 \end{aligned}$$

$$\boxed{(-2, -26) \quad (-1, -17)}$$

True or False:

21. A system of equations including a line and a parabola can have only 2 solutions. F (1 or none)

22. A system of equations including two lines can only have 0 or 1 solution. F (INFINITELY MANY)

23. A system of equations including a line and a circle can have up to 4 solutions. F (2)

24. A system of equations including 2 parabolas can have more than 2 solutions. F (up to 2)

25. $i^2 = -1$